

## Chapter 5 Section 2 Multiplication of Polynomials

### Multiplying Monomials

Multiply coefficients, and use the product rule for exponents.

Example 1: page 328

Multiply:

$$a) (5x^3y^4)(-6x^7y^8)$$

Solution:

Multiply coefficients, add exponents that have the same base

$$\begin{array}{r} (5)(-6) \\ -30 \end{array} \qquad \begin{array}{r} (x^{3+7})(y^{4+8}) \\ x^{10}y^{12} \end{array}$$

Try:

$$a) (10x^4y^3z^6)(3x^6y^3z^2)$$

### Multiplying a Monomial and Polynomial (not a Monomial)

Use the distributive property

$$\begin{array}{l} 3x^2(2x^3+5x) \\ 3x^2(2x^3)+3x^2(5x) \\ 6x^5+15x^3 \end{array}$$

Try:

$$a) 2x^4y^3(5xy^6-4x^3y^4-5)$$

### Multiply Polynomials When Neither is a Monomial

Several ways to find the product:

a) Use the distributive property

$$\begin{array}{l} (3x+7)(x^2+4x+5) \\ 3x(x^2+4x+5)+7(x^2+4x+5) \end{array}$$

**b) Vertical format**

$$\begin{array}{r} x^2 + 4x + 5 \\ 3x + 7 \\ \hline 7x^2 + 28x + 35 \\ 3x^3 + 12x^2 + 15x \\ \hline 3x^3 + 19x^2 + 43x + 35 \end{array}$$

**c) Area model**

$$(3x + 7)(x^2 + 4x + 5)$$

Set up a grid, either 2 x 3 or 3 x 2 – number of terms in each polynomial

|      |        |         |       |
|------|--------|---------|-------|
|      | $x^2$  | $4x$    | $5$   |
| $3x$ | $3x^3$ | $12x^2$ | $15x$ |
| $+7$ | $7x^2$ | $28x$   | $35$  |

Find the area of each region.

Add the like terms:  $3x^3 + 19x^2 + 43x + 35$

Try:

$$(4xy^2 + 2y)(3xy^4 - 2xy^2 + y)$$

**The Product of Two Binomials: FOIL**

$$(7x + 2)(4x + 5)$$

FOIL method

F: product of the first terms in each binomial

O: product of the outside terms

I: product of inside terms

L: product of the last terms.

Try:  $(x + 3)(2x - 4)$

**The Square of a Binomial**

$$(A+B)^2$$

Special-product formula

Square the first, +, multiply the two terms together then multiply by 2, +, square the second.

$$(A+B)^2 = A^2 + 2AB + B^2$$

Try:  $(3x+2y)^2$

**Multiplying the Sum and Difference of Two Terms(Binomials)**

$$(A+B)(A-B)$$

Can use FOIL, Area model, formula

Square the first, -, square the second

$$(A+B)(A-B) = A^2 - B^2$$

Try:  $(2x+3)(2x-3)$

**Multiplication of Polynomial Functions**

Chapter 2, defined the product of functions f and g as:

$$(fg)(x) = f(x) \cdot g(x)$$

Example 10: page 335

If  $f(x) = x - 5$ ,  $g(x) = x - 2$ , find

a)  $(fg)(x)$

b)  $(fg)(1)$

**Evaluate Functions**

Example 11

Given  $f(x) = x^2 - 7x + 3$ , find and simplify:

a)  $f(a+4)$